## II. <u>Newtonsde</u> Mechanik fer Vielteilden-Systeme

8. Newfordle Gutgleidungen & Folgerungen

8.1 Grundgleidungen

• Neutre & Massephe 
$$v = 1...N$$

$$m_{\nu} \ddot{E}_{\nu} = \frac{d}{d+} \rho_{\nu} = \frac{F}{\nu}$$

$$= F_{\nu}^{(a)} + \frac{F^{(i)}}{\sum_{\mu = 1}^{\nu} \nu_{\mu}} \dots 3N \text{ Dol. for } 3N \text{ Orts hoord.}$$

Takere innere Krafte

Krafte van den anderen Massephen: Tweiteilde

hafte

· an fire Krafte: Bap: Solwer hraft der m, Krafte aufgraf FM - Feldes

(i) Tarkere Gesamhragh 
$$\underline{F}^{(a)} = \sum_{\nu=1}^{N} \underline{F}^{(a)}_{\nu}$$
 (8.2)

(ii) "abgeschlassenes" Sisken: 
$$\underline{F}^{(a)} = 0$$
 (8.3)
in engeren Sine:  $\underline{F}^{(a)}_{\nu} = 0$ 

· june Kafte: Bep: Conlamb } hafte chem. Kindingsträfte (in Moletinien, etc...)

(i) 
$$F_{y\mu} = f_{y\mu} (\underline{r}_y - \underline{r}_\mu)$$
 ... knoft om  $m_{\mu}$  and  $m_{\nu}$   
Annahue:  $F_{y\mu} \| \underline{r}_y - \underline{r}_{\mu}$  ... Earlal highe

(ii) acho = reacho 
$$\longrightarrow \underbrace{\left[ \underbrace{F_{\nu\nu} \left( \underline{F_{\nu}} - \underline{F_{\mu\nu}} \right) - F_{\mu\nu} \left( \underline{F_{\mu}} - \underline{F_{\nu}} \right) \right]}_{P_{\nu\nu}} \left( \underbrace{R.f} \right)$$

$$\longrightarrow \underbrace{\left[ \underbrace{F_{\nu\nu}} = 0 \longrightarrow \sum_{\mu=1}^{N} \underbrace{F_{\nu\mu}} = \sum_{\mu=1}^{N} \underbrace{F_{\nu\mu}} \right]}_{p_{\nu}\neq\nu} \left( \underbrace{R.f} \right)$$

(iii) imore Gesanthaft:
$$F^{(i)} = \sum_{\nu=1}^{N} F_{\nu}^{(i)} = \sum_{\nu,\mu=1}^{N} F_{\mu\nu} \stackrel{(gt)}{=} 0$$
(8.6)

8.2 Folgengen
a) Impulsate
• Def: Gesentinguls 
$$P = \sum_{i} p_{i} = \sum_{i} m_{i} \hat{\mathbf{r}}_{i}$$
 (8.7)

$$\dot{\Sigma} (\delta A) \qquad \dot{\underline{P}} = \Sigma \dot{\underline{P}}_{\nu} = \Sigma \underline{F}_{\nu}^{(a)} + \Sigma \underline{F}_{\nu m}$$

$$= 0 \qquad [s.(8.6)]$$

Impuls sate: 
$$\frac{\dot{P}}{2e^{2}H} = \frac{\dot{F}(a)}{A} = \frac{\dot{F}(a)}{A}$$
zeith. Andry on  $P = A$ 
Sume du arginishte

Krifte

(8.9)

ab ges drossenes System:  $(F^{ca)} = 0$ :  $\dot{P} = 0 \longrightarrow P = A$ 

Nb: unabh. van Wall das 
$$KS$$
:
$$\frac{V_{\gamma}}{V_{\gamma}} = \frac{V_{\gamma}}{V_{\gamma}} + \frac{1}{2} \frac{\ln V_{\gamma}}{(e,0)} \frac{R}{R} = \frac{R'}{2} + \frac{1}{2} \frac{1}{2} \frac{\ln V_{\gamma}}{(e,0)}$$

• Schwerpht. sate:  

$$\frac{\dot{p}}{\dot{p}} = \sum_{\nu=1}^{N} m_{\nu} \ddot{r}_{\nu} = M \ddot{R} \text{ in (8.8)}$$

Bem: (i) keine fyn in (8M) -> Man ham sid nidt am
eigenen Slapf aus den Sept
zielen"

(ii) reder Korper = Masse ptt (M,R) & innere Bewe(as my) sid vie gug

(iii) r. S: inner Krift:

$$\sum_{y_{1}}\dot{E}_{y}\cdot\dot{E}_{y_{1}}=\frac{1}{2}\sum_{y_{1}}\left(\dot{x}_{y}\cdot\dot{E}_{y_{1}}+\dot{x}_{y}\cdot\dot{E}_{y_{1}}\right)$$

$$(8A) - \frac{1}{2}\sum_{y_{1}}\left[\dot{x}_{y}\cdot grad_{y}U_{y_{1}}(|x_{y}-x_{y_{1}}|)+\dot{x}_{y}\cdot grad_{y}U_{y_{1}}(|x_{y}-x_{y_{1}}|)\right]$$

$$=-\frac{1}{2}\sum_{y_{1}}\frac{d}{dt}U_{y_{1}}(|x_{y}-x_{y_{1}}|)=-\frac{d}{dt}U^{G}$$

$$Def: Gec. (Ww. energie inn Section 
$$U^{G})=\frac{1}{2}\sum_{y_{1}}U_{y_{1}}\left(|x_{y}-x_{y_{1}}|\right)$$

$$(8.20)$$

$$(1)6(i)R(ii)$$

$$dt\left(T+U^{(a)}+U^{G}\right)=O\left(8.24\right)$$

$$EES bei hours. Kriften: T+U^{(a)}+U^{G}=E\left(8.22\right)$$

$$. int dissipation Kriften: E_{y, diss}$$

$$Occurrence$$

$$dt\left[T+U^{(a)}+U^{G}\right]=\sum_{y_{2}}\frac{F_{y, diss}}{F_{y, diss}}\cdot\dot{x}_{y}$$

$$A_{12}=\sum_{y}\int_{F_{y}}F_{y}\cdot\dot{x}_{y}=\sum_{y}\int_{F_{y}}\frac{F_{y}}{F_{y}}\cdot\dot{x}_{y}dt$$

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$$A_{12}=\left(\frac{1}{2}U^{(a)}\right)-U^{(a)}\left(\frac{1}{2}U^{(a)}\right)-U^{(a)}\left(\frac{1}{2}U^{(a)}\right)$$

$$Erstandorder Gesterence$$

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$$Erstandorder Gesterence$$

$$A_{12}=\sum_{y}\int_{F_{y}}\frac{F_{y}}{F_{y}}\cdot\dot{x}_{y}dt$$

$$A_{12}=-\left[U^{(a)}\left(\frac{1}{2}U^{(a)}\right)-U^{(a)}\left(\frac{1}{2}U^{(a)}\right)-U^{(a)}\left(\frac{1}{2}U^{(a)}\right)\right]$$

$$Erstandorder Gesterence$$

$$A_{13}=\sum_{y}\int_{F_{y}}\frac{F_{y}}{F_{y}}\cdot\dot{x}_{y}dt$$

$$A_{14}=-\left[U^{(a)}\left(\frac{1}{2}U^{(a)}\right)-U^{(a)}\left(\frac{1}{2}U^{(a)}\right)-U^{(a)}\left(\frac{1}{2}U^{(a)}\right)\right]$$

$$Erstandorder Gesterence$$

$$A_{14}=-\left[U^{(a)}\left(\frac{1}{2}U^{(a)}\right)-U^{(a)}\left(\frac{1}{2}U^{(a)}\right)-U^{(a)}\left(\frac{1}{2}U^{(a)}\right)$$

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$$Erstandorder Gesterence$$

$$A_{14}=-\left[U^{(a)}\left(\frac{1}{2}U^{(a)}\right)-U^{(a)}\left(\frac{1}{2}U^{(a)}\right)$$

$$A_{15}=-\left[U^{(a)}\left(\frac{1}{2}U^{(a)}\right)-U^{(a)}\left(\frac{1}{2}U^{(a)}\right)-U^{(a)}\left(\frac{1}{2}U^{(a)}\right)$$

$$A_{15}=-\left(\frac{1}{2}U^{(a)}\right)$$

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