· Purt of Flode F: 
$$\underline{r} = \underline{r}(u, v)$$

$$d\underline{r}_{v} = \frac{\partial \underline{r}}{\partial v} dv \qquad \qquad \int_{0}^{\infty} du$$

$$d\underline{r}_{u} = \frac{\partial \underline{r}}{\partial u} du$$

$$d\underline{f} = d\underline{r}_{u} \times d\underline{r}_{v}$$

$$= \left(\frac{\partial \underline{r}}{\partial u} \times \frac{\partial \underline{r}}{\partial v}\right) du dv \qquad (7.16)$$

$$\underline{in (7.11)}$$

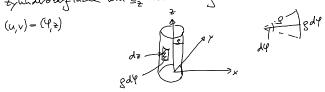
$$Q = \int \underline{a}(\underline{r}) \cdot \left(\frac{\partial \underline{r}}{\partial u} \times \frac{\partial \underline{r}}{\partial v}\right) du dv \qquad (7.17)$$

in (PM) 
$$Q = \int \underline{a}(\underline{r}) \cdot \left(\frac{\partial \underline{r}}{\partial u} \times \frac{\partial \underline{r}}{\partial v}\right) du dv \qquad (7.17)$$
... Doppel integral (s.HM)

· Box Str df.

(2) Zylindrobefläche um Ez mit Rading:

$$(u,v)=(0,\pm)$$

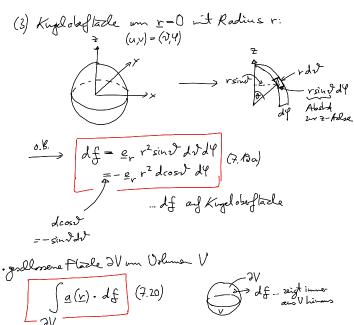


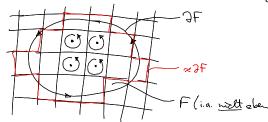
$$\underline{r} = g \underbrace{e}_{g} + \underbrace{f}_{g} \underbrace{e}_{g}$$

$$= \underbrace{e}_{g} \underbrace{cost}_{g} , g = f_{g} \underbrace{f}_{g}$$

$$\underbrace{e}_{g} = g \underbrace{e}_{g} \underbrace{f}_{g} \underbrace{f}_{g}$$

$$\underbrace{e}_{g}$$





$$\frac{d\underline{r}^{(i)} = -d\underline{r}^{i}}{d\underline{r}^{(i)} + \underline{a} \cdot d\underline{r}^{(i)}} = 0$$

tryen bei 
$$\longrightarrow Rand C = \partial F$$
 $\longrightarrow \sum_{i} \oint \underline{a} \cdot d\underline{r}^{(i)} \longrightarrow \oint \underline{a} \cdot d\underline{r}$ 

ged

a) beliefigt Weg; 
$$\int_{C} E \cdot dr = -\int_{C} gad U \cdot dr$$

$$\int_{C} u = -\int_{C} dU = -\int_{C} u \cdot du = -$$

b) gesoldsserv Weg: 
$$\underline{r}_a = \underline{r}_e \longrightarrow \oint \underline{F} \cdot \underline{J}\underline{r} = 0! (7.22)$$

$$C = \Im F$$

c) 
$$rot = -rot grad U = 0 (6.60)$$

Fort  $f \cdot df = 0$ 

(7.27)

Stokes of.

(2) Achty: 
$$\underline{v}(\underline{r}) = \frac{q_0}{9} \underline{e}_{\varphi}$$

a) rot 
$$y = 0$$
,  $y \neq 0$ 

$$\longrightarrow \int \text{rot } y \cdot df \quad \text{mich brede bar}$$

$$F \quad \text{Subs } x = 2 \cdot 2_2 \cdot EF!$$

$$\int \underline{v}(\underline{r}) \cdot d\underline{r} = \int \frac{g_0}{g} \underline{e}_{\underline{r}} \cdot \underline{g} \underline{e}_{\underline{r}} d\underline{r}$$

$$= \int \frac{g_0}{g} \underline{e}_{\underline{r}} \cdot \underline{g} \underline{e}_{\underline{r}} d\underline{r}$$

$$= g_0 \int 1 d\underline{r} = 2\pi g_0 \neq 0 !!$$

7.4 Volumen integrale

· Molivation: Gesant masse M de Erde?

Shall shifter

(i) unterdiablicles Matrial

(ii) Inhaniognitate in der

Shale

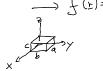


for general Kredy: 
$$\Delta V_i \longrightarrow dV \longrightarrow 0$$

• Def: Volumeninte gral aber Shalarfeld  $f(x)$  im

Uduman  $V$ 

$$\int f(x)dV \stackrel{\Delta V_i \longrightarrow dV}{=} f(x_i) \Delta V_i$$
(7.24)



$$V_{Q} = \int_{Q} dV = \iiint_{2-6} dx dy dz$$

B sp: (1) Bredne Vol. eines Quades wit Kate (age 
$$a,b,c$$
)

$$\int_{a}^{b} f(x) = 1$$

$$V_{a} = \int_{a}^{b} dV = \iint_{a}^{b} dx dy dz$$

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· beliebige Kord. 
$$x_1 x_2 x_3$$
:

(1) Kord. hafo:  $\underline{r} = \begin{pmatrix} x \\ \frac{7}{2} \end{pmatrix} = \begin{pmatrix} x (x_1 x_2 x_3) \\ y (\alpha \alpha) \end{pmatrix}$ 

(7.26)